# GEC ICP Reactor, Argon/Oxygen Chemistry

# Introduction

Electronegative discharges exhibit very different characteristics to electropositive discharges due to the presence of negative ions. Examples of electronegative gases include oxygen, nitrogen trifluoride (NF<sub>3</sub>) and sulfur hexafluoride (SF<sub>6</sub>). Details on electron gas interactions for electronegative gases can be found in Ref. 2.

The GEC cell was introduced by NIST in order to provide a standardized platform for experimental and modeling studies of discharges in different laboratories. The plasma is sustained via inductive heating. The Reference Cell operates as an inductively-coupled plasma in this model.



Figure 1: GEC ICP reactor geometry consisting of a 5 turn copper coil, plasma volume, dielectrics, and wafer with pedestal.

Note: This model requires the Plasma and AC/DC Modules.

# Model Definition

Inductively coupled discharges typically operate at low pressures (<10 Pa) and high charge density (>10<sup>17</sup> m<sup>-3</sup>). High density plasma sources are popular because low pressure ion bombardment can provide a greater degree of anisotropy on the surface of the wafer.

# DOMAIN EQUATIONS

The electron density and mean electron energy are computed by solving a pair of drift-diffusion equations for the electron density and mean electron energy. Convection of electrons due to fluid motion is neglected. For detailed information on electron transport see Theory for the Drift Diffusion User Interface in the *Plasma Module User's Guide*.

$$\frac{\partial}{\partial t}(n_e) + \nabla \cdot \left[ -n_e(\mathbf{\mu}_e \bullet \mathbf{E}) - \mathbf{D}_e \bullet \nabla n_e \right] = R_e$$
$$\frac{\partial}{\partial t}(n_{\varepsilon}) + \nabla \cdot \left[ -n_{\varepsilon}(\mathbf{\mu}_{\varepsilon} \bullet \mathbf{E}) - \mathbf{D}_{\varepsilon} \bullet \nabla n_{\varepsilon} \right] + \mathbf{E} \cdot \mathbf{\Gamma}_e = R_{\varepsilon}$$

The electron source  $R_e$  and the energy loss due to inelastic collisions  $R_{\varepsilon}$  are defined later. The electron diffusivity, energy mobility, and energy diffusivity are computed from the electron mobility using:

$$\mathbf{D}_e = \mathbf{\mu}_e T_e, \mathbf{\mu}_{\varepsilon} = \left(\frac{5}{3}\right) \mathbf{\mu}_e, \mathbf{D}_{\varepsilon} = \mathbf{\mu}_{\varepsilon} T_e$$

The source coefficients in the above equations are determined by the plasma chemistry using rate coefficients. Suppose that there are M reactions that contribute to the growth or decay of electron density and P inelastic electron-neutral collisions. In general P >> M. In the case of rate coefficients, the electron source term is given by:

$$R_e = \sum_{j=1}^{M} x_j k_j N_n n_e$$

where  $x_j$  is the mole fraction of the target species for reaction j,  $k_j$  is the rate coefficient for reaction j (SI unit: m<sup>3</sup>/s), and  $N_n$  is the total neutral number density (SI unit: 1/m<sup>3</sup>). The electron energy loss is obtained by summing the collisional energy loss over all reactions:

$$R_{\varepsilon} = \sum_{j=1}^{P} x_j k_j N_n n_e \Delta \varepsilon_j$$

where  $\Delta \varepsilon_j$  is the energy loss from reaction *j* (SI unit: V). The rate coefficients can be computed from cross section data by the following integral:

$$k_k = \gamma \int_0^\infty \varepsilon \sigma_k(\varepsilon) f(\varepsilon) d\varepsilon$$

where  $\gamma = (2q/m_e)^{1/2}$  (SI unit: C<sup>1/2</sup>/kg<sup>1/2</sup>),  $m_e$  is the electron mass (SI unit: kg),  $\varepsilon$  is energy (SI unit: V),  $\sigma_k$  is the collision cross section (SI unit: m<sup>2</sup>), and *f* is the electron energy distribution function. In this case a Maxwellian EEDF is assumed.

For non-electron species, the following equation is solved for the mass fraction of each species. For detailed information on the transport of the non-electron species see Theory for the Heavy Species Transport User Interface in the *Plasma Module User's Guide*.

$$\rho \frac{\partial}{\partial t} (w_k) + \rho (\mathbf{u} \cdot \nabla) w_k = \nabla \cdot \mathbf{j}_k + R_k$$

The electrostatic field is computed using the following equation:

$$-\nabla \cdot \varepsilon_0 \varepsilon_r \nabla V = \rho$$

The space charge density  $\rho$  is automatically computed based on the plasma chemistry specified in the model using the formula:

$$\rho = q \left( \sum_{k=1}^{N} Z_k n_k - n_e \right)$$

For detailed information about electrostatics see Theory for the Electrostatics User Interface in the *Plasma Module User's Guide*.

For a nonmagnetized, nonpolarized plasma, the induction currents are computed in the frequency domain using the following equation:

$$(j\omega\sigma - \omega^{2}\varepsilon_{0})\mathbf{A} + \nabla \times (\mu_{0}^{-1}\nabla \times \mathbf{A}) = \mathbf{J}^{e}$$
(1)

The plasma conductivity needs to be specified as a material property, usually from the cold plasma approximation:

$$\sigma = \frac{n_e q^2}{m_e (v_e + j\omega)} \tag{2}$$

where  $n_e$  is the electron density, q is the electron charge,  $m_e$  is the electron mass,  $v_e$  is the collision frequency, and  $\omega$  is the angular frequency.

# **BOUNDARY CONDITIONS**

Electrons are lost to the wall due to random motion within a few mean free paths of the wall and gained due to secondary emission effects, resulting in the following boundary condition for the electron flux:

$$-\mathbf{n} \cdot \Gamma_e = \left(\frac{1}{2} \mathbf{v}_{e, \text{ th}} n_e\right) \tag{3}$$

and the electron energy flux:

$$-\mathbf{n} \cdot \Gamma_{\varepsilon} = \left(\frac{5}{6} \mathbf{v}_{e, \text{ th}} n_{\varepsilon}\right) \tag{4}$$

The second term on the right hand side of Equation 3 is the gain of electrons due to secondary emission effects,  $\gamma_p$  being the secondary emission coefficient. The second term in Equation 4 is the secondary emission energy flux,  $\varepsilon_p$  being the mean energy of the secondary electrons. For the heavy species, ions are lost to the wall due to surface reactions and the fact that the electric field is directed towards the wall:

$$-\mathbf{n} \cdot \mathbf{j}_{k} = M_{w}R_{k} + M_{w}c_{k}Z\mu_{k}(\mathbf{E}\cdot\mathbf{n})[Z_{k}\mu_{k}(\mathbf{E}\cdot\mathbf{n}) > 0]$$
(5)

The walls of the reactor are grounded.

# PLASMA CHEMISTRY

A mixture of argon and oxygen is studied. There are 62 reactions and 15 species in the model:

REACTION	FORMULA	ТҮРЕ	$\Delta\epsilon(eV)$
I	e+O2=>e+O2	Elastic	0
2	e+O2=>O+O-	Attachment	-
3	e+O2=>e+O2	Excitation	0.02
4	e+O2=>e+O2	Excitation	0.19
5	e+O2=>e+O2	Excitation	0.19
6	e+O2=>e+O2	Excitation	0.38
7	e+O2=>e+O2	Excitation	0.38
8	e+O2=>e+O2	Excitation	0.57
9	e+O2=>e+O2	Excitation	0.75
10	e+O2=>e+O2a1d	Excitation	0.977
П	e+O2a1d=>e+O2	Excitation	-0.977
12	e+O2=>e+O2b1s	Excitation	1.627
13	e+O2b1s=>e+O2	Excitation	-1.627
14	e+O2=>e+O2(45)	Excitation	4.5
15	e+O2(45)=>e+O2	Excitation	-4.5
16	e+O2=>e+O+O	Excitation	6.0
17	e+O2=>e+O+O1d	Excitation	8.4
18	e+O2=>e+O+O1s	Excitation	9.97
19	e+O2=>2e+O2+	lonization	12.06
20	e+O2a1d=>e+O2a1d	Elastic	0
21	e+O2a1d=>e+O+O	Excitation	5.02
22	e+O2a1d=>2e+O2+	lonization	11.09
23	e+O2b1s=>e+O2b1s	Elastic	0
24	e+O2b1s=>e+O+O	Excitation	4.38
25	e+O2b1s=>2e+O2+	lonization	10.39
26	e+O2(45)=>e+O+O	Excitation	1.5
27	e+O2(45)=>2e+O2+	Ionization	7.58
28	e+O=>e+O	Elastic	0

TABLE I: TABLE OF COLLISIONS AND REACTIONS MODELED

REACTION	FORMULA	ТҮРЕ	$\Delta\epsilon(eV)$
29	e+O=>e+O1d	Excitation	1.968
30	e+OId=>e+O	Excitation	-1.968
31	e+O=>e+OIs	Excitation	4.192
32	e+OIs=>e+O	Excitation	-4.192
33	e+O=>2e+O+	Ionization	13.192
34	e+OId=>e+OIs	Excitation	2.224
35	e+OId=>2e+O+	Ionization	11.224
36	e+O1s=>2e+O+	Ionization	9.00
37	e+Ar=>e+Ar	Elastic	0
38	e+Ar=>e+Ars	Excitation	11.5
39	e+Ars=>e+Ar	Excitation	-11.5
40	e+Ar=>2e+Ar+	Ionization	15.8
41	e+Ars=>2e+Ar+	Ionization	4.427
42	e+O2+O2=>O2+O2-	Attachment	0
43	e+O2+=>O+O	Recombination	
44	e+O2+=>O+O1d	Recombination	
45	O2a1d+O2=>O2+O2	Metastable quenching	
46	O2a1d+O=>O2+O	Metastable quenching	
47	O2b1s+O2=>O2+O2	Metastable quenching	
48	O2b1s+O=>O2+O	Metastable quenching	
49	O2(45)+O2=>O2+O2	Metastable quenching	
50	Old+O2=>O+O2	Metastable quenching	
51	OId+O=>O+O2	Metastable quenching	
52	Ols+02=>0+02	Metastable quenching	
53	01s+0=>0+0	Metastable quenching	
54	0+0+02=>02+02	Recombination	
55	0+0+0=>0+02	Recombination	
56	O++O2=>O+O2+	Charge exchange	
57	O-+O=>O2+e	Detachment	
58	0-+02=>02-+0	Charge exchange	
59	0-+0+=>20	Recombination	

TABLE I: TABLE OF COLLISIONS AND REACTIONS MODELED

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REACTION	FORMULA	ТҮРЕ	$\Delta\epsilon(eV)$
60	O-+O2+=>3O	Recombination	
61	02-+02+=>202	Recombination	
62	02-+0+=>02+0	Recombination	

Negative ions cannot escape the ambipolar field, so they do not reach the reactor walls. The only way the negative ions are removed from the plasma is via recombination with positive ions. For this reason, no surface reactions need to be specified for the negative ions. The following surface reactions are included in the model:

TABLE 2: TABLE OF SURFACE REACTIONS

REACTION	FORMULA	STICKING COEFFICIENT
I	O2a1d=>O2	I
2	O2b1s=>O2	I
3	O2(45)=>O2	I
4	O2+=>O2	I
5	Old=>O	I
6	Ols=>0	I
7	O+=>O	I
8	O+O=>O2	IE-3
9	Ar+=>Ar	1
10	Ars=>Ar	I

# ELECTRICAL EXCITATION

From an electrical point of view, the GEC reactor behaves as a transformer. A current is applied to the driving coil (the primary) and this induces a current in the plasma (the secondary). The plasma then induces an opposing current back in the coil, increasing its impedance. The current flowing in the plasma depends on the current applied to the coil and the reaction kinetics. The total plasma current can vary from no current (plasma not sustained) to the same current as the primary which corresponds to perfect coupling between the coil and the plasma.

In this case, the total power absorbed by both the coil and the plasma is fixed at 2000 W. When modeling inductively coupled plasmas it is generally best to specify the total power as a setting for the coil rather than the coil current or voltage.

# Results and Discussion

The peak electron density occurs at the center of the reactor, underneath the RF coil. The electron density in this case is high enough to cause some shielding of the azimuthal electric field.



Time=0.001 Surface: Electron density (1/m<sup>3</sup>)

Figure 2: Electron density inside the GEC ICP reactor.

The electron "temperature" is highest directly underneath the coil, which is where the bulk of the power deposition occurs. The plasma potential, Figure 4, peaks at around 28 V which is in line with the expected potential for the computed electron temperature.



Figure 3: Electron "temperature" inside the GEC ICP reactor. Time=0.001 Surface: Electric potential (V)



Figure 4: Electric potential inside the GEC ICP reactor.

The velocity field is plotted in Figure 5. At these flow rates the gas does not penetrate deep into the core of the plasma. The pump causes flow of the gas down towards the wafer, then around it and out to the pump. Since inductively coupled plasmas generally operate at very low pressures, the gas flow tends to only have a small effect on the results.



Time=0.001 Surface: Velocity magnitude (m/s)

Figure 5: Velocity field in the GEC ICP reactor.

The mole fraction of atomic oxygen is plotted in Figure 6. Since the incoming gas mixture is argon and molecular oxygen, the mole fraction is lowest near the gas injector. The molecular oxygen is quickly dissociated into atomic oxygen and other electronically excited states, resulting in a higher mole fraction closer to the axis of symmetry.



Figure 6: Mole fraction of atomic oxygen inside the GEC ICP reactor.

The number density of negative ions are plotted in Figure 7 and Figure 8. The number density of O<sup>-</sup> ions is higher than  $O_2^-$  due to the fact that the dissociative attachment reaction rate (reaction number 2) is much greater than that of the 3 body attachment reaction (reaction number 42) which is the primary producer of  $O_2^-$ .



Figure 7: Number density of O<sup>-</sup> ions in the GEC ICP reactor. Time=0.001 Surface: Number density (1/m<sup>3</sup>)



Figure 8: Number density of  $O_2^-$  ions in the GEC ICP reactor.

# Notes About the COMSOL Implementation

The mobility and diffusivity of the negative ions are computed assuming that the negative ion temperature is 0.3 eV. This is a reasonable assumption, since the ions are held in the core of the plasma, where they can acquire energy from the high frequency electromagnetic field.

Due to the large number of reactions and species in the model, it requires a 64 bit machine with at least 4 GB of memory to solve.

# LIMITATIONS OF THE MODEL

The plasma chemical mechanism used in the model has not been rigorously validated against experimental measurements. If some of the reactions are removed, or additional reactions added, the results will likely change, possible significantly. It should also be noted that the mechanism used here does not include ozone or any ionic species with a molecular mass of 48 or 64. At higher pressures (above several torr), the chemical mechanism for an oxygen plasma changes dramatically. Ozone should be included, as should more exotic ionic species like  $O_3^-$  and  $O_4^+$ .

# References

1. G.J.M. Hagelaar, and L.C. Pitchford, "Solving the Boltzmann Equation to Obtain Electron Transport Coefficients and Rate Coefficients for Fluid Models," *Plasma Sources Sci. Technol*, vol. 14, pp. 722–733, 2005.

2. Loucas G. Christophorou, James K. Olthoff, "Fundamental Electron Interactions with Plasma Processing Gases", Springer, 2003.

**Model Library path:** Plasma\_Module/Inductively\_Coupled\_Plasmas/ oxygen\_gec\_icp

# Modeling Instructions

# MODEL WIZARD

- I Go to the Model Wizard window.
- 2 Click the 2D axisymmetric button.
- 3 Click Next.

- 4 In the Add physics tree, select Plasma>Inductively Coupled Plasma (icp).
- 5 Click Add Selected.
- 6 In the Add physics tree, select Fluid Flow>Single-Phase Flow>Laminar Flow (spf).
- 7 Click Add Selected.
- 8 Click Next.
- 9 Find the Studies subsection. In the tree, select Preset Studies for Selected Physics>Frequency-Transient.
- IO Click Finish.
- II In the Model Builder window's toolbar, click the Show button and select Stabilization in the menu.
- **12** In the **Model Builder** window's toolbar, click the **Show** button and select **Discretization** in the menu.

# GEOMETRY I

#### Import I

- I In the Model Builder window, under Model I right-click Geometry I and choose Import.
- 2 In the Import settings window, locate the Import section.
- **3** Click the **Browse** button.
- 4 Browse to the model's Model Library folder and double-click the file oxygen\_gec\_icp.mphbin.
- **5** Click the **Import** button.

# DEFINITIONS

Explicit I

- I In the Model Builder window, under Model I right-click Definitions and choose Selections>Explicit.
- 2 Right-click Explicit I and choose Rename.
- 3 Go to the Rename Explicit dialog box and type Walls in the New name edit field.
- 4 Click OK.
- 5 In the Explicit settings window, locate the Input Entities section.
- 6 From the Geometric entity level list, choose Boundary.
- 7 Select Boundaries 6, 8, 35–38, 44, 45, and 51–56 only.

# DEFINITIONS

# Explicit 2

- I In the Model Builder window, under Model I right-click Definitions and choose Selections>Explicit.
- 2 Right-click Explicit 2 and choose Rename.
- 3 Go to the Rename Explicit dialog box and type Coils in the New name edit field.
- 4 Click OK.
- **5** Select Domains 6 and 8–11 only.

# DEFINITIONS

# Explicit 3

- I In the Model Builder window, under Model I right-click Definitions and choose Selections>Explicit.
- 2 Right-click **Explicit 3** and choose **Rename**.
- **3** Go to the **Rename Explicit** dialog box and type **Coil Boundaries** in the **New name** edit field.
- 4 Click OK.
- **5** Select Domains 6 and 8–11 only.
- 6 In the Explicit settings window, locate the Output Entities section.
- 7 From the Output entities list, choose Adjacent boundaries.

# Explicit 4

- I In the Model Builder window, right-click Definitions and choose Selections>Explicit.
- 2 In the Explicit settings window, locate the Input Entities section.
- 3 From the Geometric entity level list, choose Boundary.
- 4 Right-click Model I>Definitions>Explicit 4 and choose Rename.
- 5 Go to the Rename Explicit dialog box and type Inlet in the New name edit field.
- 6 Click OK.
- 7 Select Boundary 44 only.

# Explicit 5

- I In the Model Builder window, right-click Definitions and choose Selections>Explicit.
- 2 In the Explicit settings window, locate the Input Entities section.
- 3 From the Geometric entity level list, choose Boundary.

- 4 Right-click Model I>Definitions>Explicit 5 and choose Rename.
- 5 Go to the Rename Explicit dialog box and type Outlet in the New name edit field.
- 6 Click OK.
- 7 Select Boundaries 35 and 37 only.

# DEFINITIONS

Variables 1

- I In the Model Builder window, under Model I right-click Definitions and choose Variables.
- 2 In the Variables settings window, locate the Variables section.
- **3** In the table, enter the following settings:

NAME	EXPRESSION	DESCRIPTION
Qin	100*tanh(1E5*t[1/s])	Inlet flow rate (sccm)
p0	0.02[Torr]	Outlet pressure

#### INDUCTIVELY COUPLED PLASMA

- I In the Model Builder window, under Model I click Inductively Coupled Plasma.
- 2 Select Domains 3–6 and 8–12 only.
- 3 In the Model Builder window, click Inductively Coupled Plasma.
- **4** In the **Inductively Coupled Plasma** settings window, locate the **Transport Settings** section.
- **5** Select the **Convection** check box.
- 6 Locate the Plasma Properties section. Select the Use reduced electron transport properties check box.
- 7 Click to expand the Discretization section. Find the Value types when using splitting of complex variables subsection. In the table, enter the following settings:

Dependent variable	Value type
Electric potential	real

Cross Section Import 1

- I Right-click Inductively Coupled Plasma and choose the domain setting Heavy Species Transport>Cross Section Import.
- 2 In the Cross Section Import settings window, locate the Cross Section Import section.
- **3** Click the **Browse** button.

4 Browse to the model's Model Library folder and double-click the file All\_02\_xsecs.txt.

## Cross Section Import 2

- I Right-click Inductively Coupled Plasma and choose the domain setting Heavy Species Transport>Cross Section Import.
- 2 In the Cross Section Import settings window, locate the Cross Section Import section.
- **3** Click the **Browse** button.
- **4** Browse to the model's Model Library folder and double-click the file Ar\_xsecs.txt.

Reaction 1

- I Right-click Inductively Coupled Plasma and choose the domain setting Heavy Species Transport>Reaction.
- 2 In the Reaction settings window, locate the Reaction Formula section.
- **3** In the **Formula** edit field, type e+02+02=>02-+02.
- 4 In the Reaction settings window, locate the Kinetics Expressions section.
- **5** In the  $k^{f}$  edit field, type 3.6e-40\*(icp.Te<sup>-</sup>-0.5)\*N\_A\_const<sup>2</sup>.

## Reaction 2

- I Right-click Inductively Coupled Plasma and choose the domain setting Heavy Species Transport>Reaction.
- 2 In the Reaction settings window, locate the Reaction Formula section.
- 3 In the Formula edit field, type e+02+=>0+0.
- 4 Locate the Kinetics Expressions section. In the k<sup>f</sup> edit field, type N\_A\_const\*1.95E-13\*(300/icp.T)^0.7.

## Reaction 3

- I Right-click Inductively Coupled Plasma and choose the domain setting Heavy Species Transport>Reaction.
- 2 In the Reaction settings window, locate the Reaction Formula section.
- 3 In the Formula edit field, type e+02+=>0+01d.
- 4 Locate the Kinetics Expressions section. In the k<sup>t</sup> edit field, type N\_A\_const\*1.95E-13\*(300/icp.T)^0.7.

#### Reaction 4

I Right-click Inductively Coupled Plasma and choose the domain setting Heavy Species Transport>Reaction.

- 2 In the Reaction settings window, locate the Reaction Formula section.
- 3 In the Formula edit field, type 02a1d+02=>02+02.
- 4 Locate the Kinetics Expressions section. In the k<sup>f</sup> edit field, type
  N A const\*3e-24\*exp(-200/icp.T).

Reaction 5

- I Right-click Inductively Coupled Plasma and choose the domain setting Heavy Species Transport>Reaction.
- 2 In the Reaction settings window, locate the Reaction Formula section.
- 3 In the Formula edit field, type 02a1d+0=>02+0.
- 4 Locate the Kinetics Expressions section. In the  $k^{f}$  edit field, type N\_A\_const\*2E-22.

## Reaction 6

- I Right-click Inductively Coupled Plasma and choose the domain setting Heavy Species Transport>Reaction.
- 2 In the Reaction settings window, locate the Reaction Formula section.
- 3 In the Formula edit field, type 02b1s+02=>02+02.
- 4 Locate the Kinetics Expressions section. In the k<sup>f</sup> edit field, type N\_A\_const\*2.317e-28\*icp.T^0.5.

Reaction 7

- I Right-click Inductively Coupled Plasma and choose the domain setting Heavy Species Transport>Reaction.
- 2 In the Reaction settings window, locate the Reaction Formula section.
- 3 In the Formula edit field, type 02b1s+0=>02+0.
- 4 Locate the Kinetics Expressions section. In the k<sup>f</sup> edit field, type N\_A\_const\*4.634e-22\*icp.T^0.5.

Reaction 8

- I Right-click Inductively Coupled Plasma and choose the domain setting Heavy Species Transport>Reaction.
- 2 In the Reaction settings window, locate the Reaction Formula section.
- **3** In the **Formula** edit field, type 0245+02=>02+02.
- 4 Locate the Kinetics Expressions section. In the  $k^{f}$  edit field, type N\_A\_const\*2E-19.

# Reaction 9

- I Right-click Inductively Coupled Plasma and choose the domain setting Heavy Species Transport>Reaction.
- 2 In the **Reaction** settings window, locate the **Reaction Formula** section.
- 3 In the Formula edit field, type 01d+02=>0+02.
- 4 Locate the Kinetics Expressions section. In the k<sup>f</sup> edit field, type N\_A\_const\*3.2e-17\*exp(67/icp.T).

## Reaction 10

- I Right-click Inductively Coupled Plasma and choose the domain setting Heavy Species Transport>Reaction.
- 2 In the Reaction settings window, locate the Reaction Formula section.
- **3** In the **Formula** edit field, type 01d+0=>0+0.
- 4 Locate the Kinetics Expressions section. In the k<sup>f</sup> edit field, type N\_A\_const\*8.0E-18.

# Reaction 11

- I Right-click Inductively Coupled Plasma and choose the domain setting Heavy Species Transport>Reaction.
- 2 In the Reaction settings window, locate the Reaction Formula section.
- 3 In the Formula edit field, type 01s+02=>0+02.
- 4 Locate the Kinetics Expressions section. In the k<sup>f</sup> edit field, type N\_A\_const\*4.8e-18\*exp(67/icp.T).

# Reaction 12

- I Right-click Inductively Coupled Plasma and choose the domain setting Heavy Species Transport>Reaction.
- 2 In the Reaction settings window, locate the Reaction Formula section.
- 3 In the Formula edit field, type 01s+0=>0+0.
- **4** Locate the **Kinetics Expressions** section. In the  $k^{f}$  edit field, type N\_A\_const\*3.33E-17\*exp(-300/icp.T).

# Reaction 13

- I Right-click Inductively Coupled Plasma and choose the domain setting Heavy Species Transport>Reaction.
- 2 In the Reaction settings window, locate the Reaction Formula section.
- **3** In the **Formula** edit field, type 0+0+02=>02+02.

4 Locate the Kinetics Expressions section. In the k<sup>f</sup> edit field, type
 N A const<sup>2</sup>\*9.268e-42\*(icp.T<sup>-0.63</sup>).

# Reaction 14

- I Right-click Inductively Coupled Plasma and choose the domain setting Heavy Species Transport>Reaction.
- 2 In the Reaction settings window, locate the Reaction Formula section.
- **3** In the **Formula** edit field, type 0+0+0=>0+02.
- 4 Locate the Kinetics Expressions section. In the k<sup>f</sup> edit field, type
  N A const^2\*3.334e-41\*(icp.T^-0.63).

#### Reaction 15

- I Right-click Inductively Coupled Plasma and choose the domain setting Heavy Species Transport>Reaction.
- 2 In the Reaction settings window, locate the Reaction Formula section.
- **3** In the **Formula** edit field, type 0++02=>0+02+.
- 4 Locate the Kinetics Expressions section. In the k<sup>f</sup> edit field, type N\_A\_const\*1.9E-18\*icp.T^-0.4.

## Reaction 16

- I Right-click Inductively Coupled Plasma and choose the domain setting Heavy Species Transport>Reaction.
- 2 In the Reaction settings window, locate the Reaction Formula section.
- 3 In the Formula edit field, type 0-+0=>02+e.
- 4 Locate the Kinetics Expressions section. In the k<sup>f</sup> edit field, type N\_A\_const\*5.0E-16.

## Reaction 17

- I Right-click Inductively Coupled Plasma and choose the domain setting Heavy Species Transport>Reaction.
- 2 In the Reaction settings window, locate the Reaction Formula section.
- 3 In the Formula edit field, type 0-+02=>02-+0.
- 4 Locate the Kinetics Expressions section. In the k<sup>f</sup> edit field, type N\_A\_const\*1.0E-20.

#### Reaction 18

I Right-click Inductively Coupled Plasma and choose the domain setting Heavy Species Transport>Reaction.

- 2 In the Reaction settings window, locate the Reaction Formula section.
- 3 In the Formula edit field, type 0-+0+=>20.
- 4 Locate the Kinetics Expressions section. In the  $k^{f}$  edit field, type N\_A\_const\*2.3E-13\*(icp.T/300)^-0.5.

Reaction 19

- I Right-click Inductively Coupled Plasma and choose the domain setting Heavy Species Transport>Reaction.
- 2 In the Reaction settings window, locate the Reaction Formula section.
- 3 In the Formula edit field, type 0-+02+=>30.
- 4 Locate the Kinetics Expressions section. In the k<sup>f</sup> edit field, type N A const\*2.3E-13\*(icp.T/300)^-0.5.

Reaction 20

- I Right-click Inductively Coupled Plasma and choose the domain setting Heavy Species Transport>Reaction.
- 2 In the **Reaction** settings window, locate the **Reaction Formula** section.
- 3 In the Formula edit field, type 02-+02+=>202.
- 4 Locate the Kinetics Expressions section. In the k<sup>f</sup> edit field, type N\_A\_const\*2.3E-13\*(icp.T/300)^-0.5.

Reaction 21

- I Right-click Inductively Coupled Plasma and choose the domain setting Heavy Species Transport>Reaction.
- 2 In the Reaction settings window, locate the Reaction Formula section.
- 3 In the Formula edit field, type 02 +0 + = > 02 + 0.
- 4 Locate the Kinetics Expressions section. In the k<sup>f</sup> edit field, type
  N A const\*2.3E-13\*(icp.T/300)^-0.5.

Plasma Model I

- I In the Model Builder window, under Model I>Inductively Coupled Plasma click Plasma Model I.
- 2 In the Plasma Model settings window, locate the Model Inputs section.
- **3** From the **u** list, choose **Velocity field (spf/fpl)**.
- **4** In the *T* edit field, type 500[K].
- **5** From the  $p_A$  list, choose **Pressure (spf/fpl)**.

- 6 Clear the **Reference pressure** check box.
- 7 Locate the Electron Density and Energy section. In the  $\mu_e N_n$  edit field, type 4E24.

# Initial Values 1

- I In the Model Builder window, under Model I>Inductively Coupled Plasma click Initial Values I.
- 2 In the Initial Values settings window, locate the Initial Values section.
- **3** In the  $n_{e,0}$  edit field, type 1E15.
- **4** In the  $\varepsilon_0$  edit field, type **5**.

## Surface Reaction 1

- I In the Model Builder window, right-click Inductively Coupled Plasma and choose the boundary condition Heavy Species Transport>Surface Reaction.
- 2 In the Surface Reaction settings window, locate the Reaction Formula section.
- **3** In the **Formula** edit field, type 02a1d=>02.
- 4 Locate the Boundary Selection section. From the Selection list, choose Walls.

#### Surface Reaction 2

- I Right-click Inductively Coupled Plasma and choose the boundary condition Heavy Species Transport>Surface Reaction.
- 2 In the Surface Reaction settings window, locate the Reaction Formula section.
- 3 In the Formula edit field, type 02b1s=>02.
- 4 Locate the Boundary Selection section. From the Selection list, choose Walls.

## Surface Reaction 3

- I Right-click Inductively Coupled Plasma and choose the boundary condition Heavy Species Transport>Surface Reaction.
- 2 In the Surface Reaction settings window, locate the Reaction Formula section.
- 3 In the Formula edit field, type 0245=>02.
- 4 Locate the Boundary Selection section. From the Selection list, choose Walls.

## Surface Reaction 4

- I Right-click Inductively Coupled Plasma and choose the boundary condition Heavy Species Transport>Surface Reaction.
- 2 In the Surface Reaction settings window, locate the Reaction Formula section.
- 3 In the Formula edit field, type 02+=>02.
- 4 Locate the Boundary Selection section. From the Selection list, choose Walls.

# Surface Reaction 5

- I Right-click Inductively Coupled Plasma and choose the boundary condition Heavy Species Transport>Surface Reaction.
- 2 In the Surface Reaction settings window, locate the Reaction Formula section.
- 3 In the Formula edit field, type 01d=>0.
- 4 Locate the Boundary Selection section. From the Selection list, choose Walls.

# Surface Reaction 6

- I Right-click Inductively Coupled Plasma and choose the boundary condition Heavy Species Transport>Surface Reaction.
- 2 In the Surface Reaction settings window, locate the Reaction Formula section.
- **3** In the **Formula** edit field, type 01s=>0.
- 4 Locate the Boundary Selection section. From the Selection list, choose Walls.

## Surface Reaction 7

- I Right-click Inductively Coupled Plasma and choose the boundary condition Heavy Species Transport>Surface Reaction.
- 2 In the Surface Reaction settings window, locate the Reaction Formula section.
- **3** In the **Formula** edit field, type 0+=>0.
- 4 Locate the Boundary Selection section. From the Selection list, choose Walls.

#### Surface Reaction 8

- I Right-click Inductively Coupled Plasma and choose the boundary condition Heavy Species Transport>Surface Reaction.
- 2 In the Surface Reaction settings window, locate the Reaction Formula section.
- 3 In the Formula edit field, type 0+0=>0.502.
- 4 Locate the Boundary Selection section. From the Selection list, choose Walls.
- **5** Locate the **Kinetics Expressions** section. In the  $\gamma_f$  edit field, type 1E-3.

#### Surface Reaction 9

- I Right-click Inductively Coupled Plasma and choose the boundary condition Heavy Species Transport>Surface Reaction.
- 2 In the Surface Reaction settings window, locate the Reaction Formula section.
- **3** In the **Formula** edit field, type Ar+=>Ar.
- 4 Locate the Boundary Selection section. From the Selection list, choose Walls.

# Surface Reaction 10

- I Right-click Inductively Coupled Plasma and choose the boundary condition Heavy Species Transport>Surface Reaction.
- 2 In the Surface Reaction settings window, locate the Reaction Formula section.
- 3 In the Formula edit field, type Ars=>Ar.
- 4 Locate the Boundary Selection section. From the Selection list, choose Walls.

# Ampère's Law 1

- I Right-click Inductively Coupled Plasma and choose the domain setting Magnetic Fields>Ampère's Law.
- 2 Select Domains 4–6 and 8–12 only.

# Wall I

- I Right-click Inductively Coupled Plasma and choose the boundary condition Drift Diffusion>Wall.
- 2 In the Wall settings window, locate the General Wall Settings section.
- **3** In the  $r_e$  edit field, type **0**.
- 4 Select Boundaries 6, 8, 35–38, 44, 45, and 51–56 only.
- 5 Locate the Boundary Selection section. From the Selection list, choose Walls.

# Ground I

- I Right-click Inductively Coupled Plasma and choose the boundary condition Electrostatics>Ground.
- **2** Select Boundaries 6, 8, 35–38, 44, 45, and 51–56 only.

# Coil Group Domain I

- I Right-click Inductively Coupled Plasma and choose the domain setting Magnetic Fields>Coil Group Domain.
- 2 Select Domains 6 and 8–11 only.
- 3 In the Coil Group Domain settings window, locate the Coil Group Domain section.
- 4 From the Coil excitation list, choose Power.
- **5** In the  $P_{\text{coil}}$  edit field, type 2000[W].

# Species: O2

- In the Model Builder window, under Model I>Inductively Coupled Plasma click Species:
  02.
- 2 In the Species settings window, locate the Species Formula section.

3 Select the From mass constraint check box.

4 Locate the General Parameters section. From the Preset species data list, choose 02.

# Species: O

- In the Model Builder window, under Model I>Inductively Coupled Plasma click Species:
  0.
- 2 In the Species settings window, locate the General Parameters section.
- 3 From the Preset species data list, choose 0.

## Inlet 1

- I In the Model Builder window, right-click Species: O and choose Inlet.
- 2 In the Inlet settings window, locate the Boundary Selection section.
- 3 From the Selection list, choose Inlet.
- 4 Locate the Inlet section. From the Mixture specification list, choose Mole fraction.
- **5** In the  $x_0$  edit field, type 1E-8.

## Outflow I

- I In the Model Builder window, under Model I>Inductively Coupled Plasma right-click Species: O and choose Outflow.
- 2 In the Outflow settings window, locate the Boundary Selection section.
- **3** From the **Selection** list, choose **Outlet**.

# Species: O-

- In the Model Builder window, under Model I>Inductively Coupled Plasma click Species:
  0-.
- 2 In the Species settings window, locate the General Parameters section.
- 3 From the Preset species data list, choose 0.
- 4 Click to expand the Mobility and Diffusivity Expressions section. From the Ion temperature list, choose Specify ion temperature.
- **5** In the *T<sub>ion</sub>* edit field, type 0.3[V]\*e\_const/k\_B\_const.

# Species: O2ald

- I In the Model Builder window, under Model I>Inductively Coupled Plasma click Species: 02ald.
- 2 In the Species settings window, locate the General Parameters section.
- 3 From the Preset species data list, choose 02.

## Species: O2b1s

- I In the Model Builder window, under Model I>Inductively Coupled Plasma click Species: 02b1s.
- 2 In the Species settings window, locate the General Parameters section.
- 3 From the Preset species data list, choose 02.

## Species: 0245

- I In the Model Builder window, under Model I>Inductively Coupled Plasma click Species: 0245.
- 2 In the Species settings window, locate the General Parameters section.
- 3 From the Preset species data list, choose 02.

#### Species: OId

- I In the Model Builder window, under Model I>Inductively Coupled Plasma click Species: Old.
- 2 In the Species settings window, locate the General Parameters section.
- **3** From the **Preset species data** list, choose **0**.

#### Species: OIs

- I In the Model Builder window, under Model I>Inductively Coupled Plasma click Species: OIs.
- 2 In the Species settings window, locate the General Parameters section.
- 3 From the Preset species data list, choose 0.

## Species: 02+

- I In the Model Builder window, under Model I>Inductively Coupled Plasma click Species: 02+.
- 2 In the Species settings window, locate the General Parameters section.
- 3 From the Preset species data list, choose 02.
- **4** Locate the **Species Formula** section. Select the **Initial value from electroneutrality constraint** check box.

# Species: O+

- In the Model Builder window, under Model I>Inductively Coupled Plasma click Species:
  0+.
- 2 In the Species settings window, locate the General Parameters section.
- 3 From the Preset species data list, choose 0.

# Species: Ar

- I In the Model Builder window, under Model I>Inductively Coupled Plasma click Species: Ar.
- 2 In the Species settings window, locate the General Parameters section.
- 3 From the Preset species data list, choose Ar.
- **4** In the  $x_0$  edit field, type **0.3**.

# Inlet 1

- I In the Model Builder window, right-click Species: Ar and choose Inlet.
- 2 In the Inlet settings window, locate the Boundary Selection section.
- 3 From the Selection list, choose Inlet.
- **4** Locate the **Inlet** section. From the **Mixture specification** list, choose **Mole fraction**.
- **5** In the  $x_0$  edit field, type 0.3.

#### Outflow I

- I In the Model Builder window, under Model I>Inductively Coupled Plasma right-click Species: Ar and choose Outflow.
- 2 In the Outflow settings window, locate the Boundary Selection section.
- 3 From the Selection list, choose Outlet.

#### Species: Ars

- I In the Model Builder window, under Model I>Inductively Coupled Plasma click Species: Ars.
- 2 In the Species settings window, locate the General Parameters section.
- 3 From the Preset species data list, choose Ar.

## Species: Ar+

- I In the Model Builder window, under Model I>Inductively Coupled Plasma click Species: Ar+.
- 2 In the Species settings window, locate the General Parameters section.
- 3 From the Preset species data list, choose Ar.

#### Species: O2-

- I In the Model Builder window, under Model I>Inductively Coupled Plasma click Species: 02-.
- 2 In the Species settings window, locate the General Parameters section.
- 3 From the Preset species data list, choose 02.

- 4 Click to expand the Mobility and Diffusivity Expressions section. From the Ion temperature list, choose Specify ion temperature.
- 5 In the T<sub>ion</sub> edit field, type 0.3[V]\*e\_const/k\_B\_const.

# LAMINAR FLOW

- I In the Model Builder window, under Model I click Laminar Flow.
- 2 In the Laminar Flow settings window, locate the Consistent Stabilization section.
- **3** Find the Navier-Stokes equations subsection. Clear the Crosswind diffusion check box.
- 4 Locate the Domain Selection section. Click Clear Selection.
- **5** Select Domain 3 only.
- 6 Click to expand the Equation section. From the Equation form list, choose Stationary.

## Fluid Properties 1

- I In the Model Builder window, under Model I>Laminar Flow click Fluid Properties I.
- 2 In the Fluid Properties settings window, locate the Fluid Properties section.
- **3** From the  $\rho$  list, choose **Density (icp/pem1)**.
- 4 From the  $\mu$  list, choose Dynamic viscosity (icp/peml).

#### Initial Values 1

- I In the Model Builder window, under Model I>Laminar Flow click Initial Values I.
- 2 In the Initial Values settings window, locate the Initial Values section.
- **3** In the *p* edit field, type p0.

## Inlet 1

- I In the Model Builder window, right-click Laminar Flow and choose Inlet.
- 2 In the Inlet settings window, locate the Boundary Selection section.
- **3** From the **Selection** list, choose **Inlet**.
- 4 In the Inlet settings window, locate the Boundary Condition section.
- 5 From the Boundary condition list, choose Mass flow.
- 6 Locate the Mass Flow Rate section. From the Mass flow type list, choose Standard flow rate (SCCM).
- 7 In the  $Q_{\text{sccm}}$  edit field, type Qin.
- 8 From the  $M_n$  list, choose Mean molar mass (icp/peml).

# Outlet I

I Right-click Laminar Flow and choose Outlet.

- 2 In the Outlet settings window, locate the Boundary Selection section.
- 3 From the Selection list, choose Outlet.
- **4** Locate the **Boundary Condition** section. In the  $p_0$  edit field, type p0.

# Inlet 1

Now you assign material properties to the plasma, air, coil and dielectric domains.

# MATERIALS

Material I

- I In the Model Builder window, under Model I right-click Materials and choose Material.
- 2 In the Material settings window, locate the Geometric Entity Selection section.
- 3 From the Selection list, choose Coils.
- 4 Locate the Material Contents section. In the table, enter the following settings:

Property	Name	Value
Electrical conductivity	sigma	6e7
Relative permittivity	epsilonr	1
Relative permeability	mur	1

Material 2

- I In the Model Builder window, right-click Materials and choose Material.
- 2 Select Domains 4, 5, and 12 only.
- 3 In the Material settings window, locate the Material Contents section.
- **4** In the table, enter the following settings:

Property	Name	Value
Electrical conductivity	sigma	0
Relative permittivity	epsilonr	1
Relative permeability	mur	1

# MESH I

Meshing is a critical step in any plasma model. Boundary layer meshing on the reactor walls is nearly always necessary. This is needed to capture the separation of space charge between the electrons and ions close to the wall. You also add a fine mesh in the coil domains since the skin effect needs to be resolved.

I In the Model Builder window, click Mesh I.

- 2 In the Mesh settings window, locate the Mesh Settings section.
- 3 From the Element size list, choose Finer.

# Edge 1

- I Right-click Mesh I and choose Edge.
- **2** Select Boundaries 6, 8, 44, 45, and 54 only.

## Size 1

- I Right-click Model I>Mesh I>Edge I and choose Size.
- 2 In the Size settings window, locate the Geometric Entity Selection section.
- 3 From the Geometric entity level list, choose Entire geometry.
- 4 Locate the **Element Size** section. Click the **Custom** button.
- **5** Locate the **Element Size Parameters** section. Select the **Maximum element size** check box.
- 6 In the associated edit field, type 1E-3.

# Free Triangular 1

- I In the Model Builder window, right-click Mesh I and choose Free Triangular.
- 2 In the Free Triangular settings window, locate the Domain Selection section.
- 3 From the Geometric entity level list, choose Domain.
- 4 Select Domain 3 only.

## Size 1

- I Right-click Model I>Mesh I>Free Triangular I and choose Size.
- 2 In the Size settings window, locate the Element Size section.
- 3 From the Predefined list, choose Extra fine.

## Boundary Layers 1

- I In the Model Builder window, right-click Mesh I and choose Boundary Layers.
- 2 In the Boundary Layers settings window, locate the Domain Selection section.
- 3 From the Geometric entity level list, choose Domain.
- **4** Select Domain 3 only.

## Boundary Layer Properties

I In the Model Builder window, under Model I>Mesh I>Boundary Layers I click Boundary Layer Properties.

- **2** In the **Boundary Layer Properties** settings window, locate the **Boundary Selection** section.
- 3 From the Selection list, choose Walls.
- **4** Locate the **Boundary Layer Properties** section. In the **Number of boundary layers** edit field, type **5**.
- 5 In the Boundary layer stretching factor edit field, type 1.4.

# Mapped I

- I In the Model Builder window, right-click Mesh I and choose Mapped.
- 2 In the Mapped settings window, locate the Domain Selection section.
- **3** From the Geometric entity level list, choose Domain.
- 4 From the Selection list, choose Coils.

## Distribution I

- I Right-click Model I>Mesh I>Mapped I and choose Distribution.
- 2 In the Distribution settings window, locate the Boundary Selection section.
- **3** From the Selection list, choose Coil Boundaries.
- **4** In the **Distribution** settings window, locate the **Distribution** section.
- **5** From the **Distribution properties** list, choose **Predefined distribution type**.
- 6 In the Number of elements edit field, type 30.
- 7 In the **Element ratio** edit field, type 10.
- 8 From the Distribution method list, choose Geometric sequence.
- **9** Select the **Symmetric distribution** check box.

## Free Triangular 2

- I In the Model Builder window, right-click Mesh I and choose Free Triangular.
- 2 Right-click Mesh I and choose Build All.
- 3 Click the Zoom Extents button on the Graphics toolbar.

# STUDY I

The model is now ready to be solved. You just need to enter the list of output times and the frequency for the induction currents.

# Step 1: Frequency-Transient

I In the Model Builder window, expand the Study I node, then click Step I: Frequency-Transient.

- 2 In the Frequency-Transient settings window, locate the Study Settings section.
- 3 In the Times edit field, type 0.
- 4 Click the **Range** button.
- 5 Go to the Range dialog box.
- 6 From the Entry method list, choose Number of values.
- 7 In the Start edit field, type -8.
- 8 In the **Stop** edit field, type -3.
- 9 In the Number of values edit field, type 11.
- **IO** From the **Function to apply to all values** list, choose **expIO**.
- II Click the **Add** button.
- 12 In the Frequency-Transient settings window, locate the Study Settings section.
- **I3** In the **Frequency** edit field, type **13.56E6**.

#### Solver I

- I In the Model Builder window, right-click Study I and choose Show Default Solver.
- 2 Expand the Solver I node.
- 3 In the Model Builder window, under Study I>Solver Configurations>Solver I click Time-Dependent Solver I.
- **4** In the **Time-Dependent Solver** settings window, click to expand the **Absolute Tolerance** section.
- 5 From the Global method list, choose Unscaled.
- 6 Right-click Study I>Solver Configurations>Solver I>Time-Dependent Solver I and choose Segregated.
- 7 In the Model Builder window, expand the Study I>Solver Configurations>SolverI>Time-Dependent Solver I>Segregated I node, then click Segregated Step.
- 8 In the Segregated Step settings window, locate the General section.
- 9 In the Variables list, choose Velocity field (mod1.u), Pressure (mod1.p), and mod1.spf.Pmfinl11.
- **IO** Under **Variables**, click **Delete**.
- II Click to expand the Method and Termination section. From the Jacobian update list, choose On every iteration.
- I2 In the Model Builder window, under Study I>Solver Configurations>Solver
  I>Time-Dependent Solver I right-click Segregated I and choose Segregated Step.

- **I3** In the Segregated Step settings window, locate the General section.
- **I4** Under **Variables**, click **Add**.
- **I5** Go to the **Add** dialog box.
- I6 In the Variables list, choose Velocity field (modl.u), Pressure (modl.p), and modl.spf.Pmfinlll.
- **I7** Click the **OK** button.
- **18** In the **Segregated Step** settings window, locate the **Method and Termination** section.
- 19 From the Jacobian update list, choose Once per time step.

20 In the Model Builder window, right-click Study I and choose Compute.

21 Click the Zoom Extents button on the Graphics toolbar.

# RESULTS

# Velocity (spf) I

- I In the Model Builder window, under Results right-click Velocity (spf) and choose Duplicate.
- 2 Right-click Velocity (spf) I and choose Rename.
- **3** Go to the **Rename 2D Plot Group** dialog box and type Atomic Oxygen in the **New** name edit field.
- 4 Click OK.

Atomic Oxygen

- I In the Model Builder window, expand the Results>Atomic Oxygen node, then click Surface I.
- 2 In the Surface settings window, click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Inductively Coupled Plasma (Heavy Species Transport)>Mole fractions>Mole fraction (icp.x\_w0).
- 3 Click the **Plot** button.

# 2D Plot Group 8

- I In the Model Builder window, right-click Results and choose 2D Plot Group.
- 2 Right-click 2D Plot Group 8 and choose Surface.
- 3 In the Surface settings window, click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Inductively Coupled Plasma (Heavy Species Transport)>Number densities>Number density (icp.n\_w0\_1m).
- **4** Click the **Plot** button.

# 2D Plot Group 9

- I In the Model Builder window, right-click 2D Plot Group 8 and choose Duplicate.
- 2 In the Model Builder window, expand the 2D Plot Group 9 node, then click Surface 1.
- 3 In the Surface settings window, click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Inductively Coupled Plasma (Heavy Species Transport)>Number densities>Number density (icp.n\_w02\_1m).
- **4** Click the **Plot** button.