

# Unsteady 3D Flow Past a Cylinder

Fluid flow past a cylinder is a common test case in computational fluid dynamics. The flow pattern is characterized by the Reynolds number which is defined as

$$\operatorname{Re} = \frac{\rho U_{\text{mean}} D}{\mu}$$

where  $\rho$  is the density,  $U_{\text{mean}}$  is the mean velocity of the free stream, D is the cylinder diameter, and  $\mu$  is the dynamic viscosity.

The flow patterns around a cylinder in a free stream for different Reynolds numbers are shown in Ref. 1. At Re below 5, the flow remains attached to the cylinder. For Re between 5 and 15, steady wake vortices start forming on the downstream side of the cylinder. The wake becomes unsteady and forms a laminar vortex street for Re between 40 and 150.

Flow around a cylinder in a channel is even more complicated due to the effect of wall boundaries. Computer simulations of this problem at the intermediate Re regime (between 40 and 150) are challenging since they need to be 3D and time-dependent.

In this verification model, a benchmark problem of unsteady, incompressible 3D flow past a cylinder for Re = 100 during a period of 8 seconds is considered. The lift and drag coefficients are computed and are compared with those in Ref. 2.

# Model Definition

The geometry is a cylinder of radius R with the axis parallel to the *z*-axis, and placed at  $(x_c, y_c, 0)$ , inside the box  $[0, L] \times [0, H] \times [0, H]$ . Figure 1 shows the geometry corresponding to R = 0.05 m, L = 2.5 m, H = 0.5 m, and  $x_c = 0.5$  m,  $y_c = 0.2$  m.

The fluid to be considered is incompressible and Newtonian with a kinematic viscosity of  $10^{-3}$  m<sup>2</sup>/s. The inflow velocity profile varies in time according to

$$U(0, y, z, t) = 36 U_{\text{mean}} yz \frac{(H-y)(H-z)}{H^4} \sin\left(\frac{\pi t}{8}\right), V=W=0.$$

The lift and drag coefficients  $C_{\rm D}$  and  $C_{\rm L}$  are computed as functions of time,

$$C_{\rm D}(t) = \frac{2F_{\rm D}(t)}{\rho U_{\rm mean}^2 A}, \qquad C_{\rm L}(t) = \frac{2F_{\rm L}(t)}{\rho U_{\rm mean}^2 A}$$

where  $F_{\rm D}$  and  $F_{\rm L}$  are the drag and lift forces, and A is the projected area, A = 2RH.

#### 2 | UNSTEADY 3D FLOW PAST A CYLINDER



Figure 1: The geometry is a cylinder placed inside a box.

The simulation is performed with a relatively coarse mesh with 7200 hexahedral elements shown in Figure 2. P2+P2 shape functions are chosen for the velocity and pressure to allow for better conservation and higher accuracy compared to P2+P1 and P1+P1. The generalized alpha method with automatic time stepping is chosen since it has less damping than the BDF method.



Figure 2: The relatively coarse mesh, with 7200 hexahedral elements, used in the simulation.

Figure 3 shows the flow pattern at t = 7.95 s, the last saved time before the inflow velocity returns to zero.

The lift and drag coefficients versus time are shown in Figure 4 and Figure 5 respectively. They capture the general shape of those published Ref. 1 quite well. Note that the nonzero drag at t = 0 s is due to the initial acceleration at the inlet boundary.

In order to verify the results, the L2 norm is computed for the lift and drag coefficients over the entire solved time-span. The results are consistent with those published Ref. 2. The relative error in lift is around 12% and the relative error in drag is approximately 1.2%.

When the mesh size is reduced by a factor of 2, resulting in 57,600 elements, the computational time increases by a factor of 8 but the agreement with the current simulation is still excellent.

Time=7.95 s Slice: Velocity magnitude (m/s) Streamline: Velocity field Surface: 1 (1)



Figure 3: Computed velocity field at t = 7.95 s.



Figure 4: Lift coefficient versus time.



Figure 5: Drag coefficient versus time.

The space discretization P2+P2 coupled with the generalized alpha time discretization works efficiently for this application. P2+P2 elements allow for a coarser mesh, better conservation, and more accuracy compared to P2+P1 and P1+P1 elements. The generalized alpha method has less damping than the BDF method. Automatic time-stepping works well and relatively large time steps can be used, and thus less computational time is needed compared to Ref. 2.

# References

1. M. Van Dyke, *An album of fluid motion*, the Parabolic Press, ISBN 0-915760-03-7, 1982.

2. E. Bayraktar, O. Mierka, and S. Turek, "Benchmark Computation of 3D Laminar Flow Around a Cylinder with CFX, OpenFOAM and FeatFlow," *IJCSE*, vol. 7, no. 3, pp. 253–266, 2012.

**Application Library path:** CFD\_Module/Verification\_Examples/ cylinder\_flow\_3d\_periodic

# Modeling Instructions

From the File menu, choose New.

# NEW

In the New window, click 🙆 Model Wizard.

#### MODEL WIZARD

- I In the Model Wizard window, click 间 3D.
- 2 In the Select Physics tree, select Fluid Flow > Single-Phase Flow > Laminar Flow (spf).
- 3 Click Add.
- 4 Click 🔿 Study.
- 5 In the Select Study tree, select General Studies > Time Dependent.
- 6 Click 🗹 Done.

# GLOBAL DEFINITIONS

# Parameters 1

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.

**3** In the table, enter the following settings:

Name	Expression	Value	Description
U_mean	1[m/s]	I m/s	Mean inflow velocity
rho	1[kg/m^3]	I kg/m³	Density
mu	0.001[Pa*s]	0.001 Pa·s	Dynamic viscosity
Н	0.41[m]	0.41 m	Height and Width
L	2.5[m]	2.5 m	Length
xc	0.5[m]	0.5 m	Cylinder x-pos
ус	0.2[m]	0.2 m	Cylinder y-pos
R	0.05[m]	0.05 m	Cylinder radius
dt	0.05	0.05	
Ν	160	160	
final	N*dt	8	

# GEOMETRY I

First, create the box  $[0, L] \times [0, H] \times [0, H]$ .

Block I (blk1)

- I In the **Geometry** toolbar, click 🗍 **Block**.
- 2 In the Settings window for Block, locate the Size and Shape section.
- 3 In the Width text field, type L.
- 4 In the **Depth** text field, type H.
- 5 In the Height text field, type H.

Next, create a smaller box around the cylinder. This box will be used later on in the meshing sequence.

Block 2 (blk2)

- I In the **Geometry** toolbar, click 🗍 Block.
- 2 In the Settings window for Block, locate the Size and Shape section.
- 3 In the Width text field, type 4\*R.

- 4 In the **Depth** text field, type 4\*R.
- 5 In the Height text field, type H.
- 6 Locate the Position section. In the x text field, type xc-2\*R.
- 7 In the y text field, type yc-2\*R.

Now, create the cylinder.

#### Cylinder I (cyl1)

- I In the **Geometry** toolbar, click 📗 **Cylinder**.
- 2 In the Settings window for Cylinder, locate the Size and Shape section.
- 3 In the Radius text field, type R.
- 4 In the **Height** text field, type H.
- **5** Locate the **Position** section. In the **x** text field, type **xc**.
- 6 In the y text field, type yc.
- 7 Locate the Rotation Angle section. In the Rotation text field, type 45.
- 8 In the Geometry toolbar, click 🟢 Build All.

The following operations divide the flow domain into a number of subdomains. This way, a coarser mesh can be used far from the cylinder.

# Line Segment I (Is I)

- I In the Geometry toolbar, click  $\bigoplus$  More Primitives and choose Line Segment.
- 2 On the object cyll, select Point 2 only.
- 3 In the Settings window for Line Segment, locate the Endpoint section.
- **4** Click to select the **Delta Activate Selection** toggle button for **End vertex**.
- 5 On the object **blk2**, select Point 5 only.

# Line Segment 2 (Is2)

- I In the **Geometry** toolbar, click  $\bigoplus$  **More Primitives** and choose **Line Segment**.
- **2** On the object **cyll**, select Point 6 only.
- 3 In the Settings window for Line Segment, locate the Endpoint section.
- **4** Click to select the **E** Activate Selection toggle button for **End vertex**.
- **5** On the object **blk2**, select Point 7 only.

#### Line Segment 3 (Is3)

- I In the **Geometry** toolbar, click  $\bigoplus$  **More Primitives** and choose **Line Segment**.
- 2 On the object cyll, select Point 8 only.

- 3 In the Settings window for Line Segment, locate the Endpoint section.
- **4** Click to select the **E** Activate Selection toggle button for **End vertex**.
- 5 On the object **blk2**, select Point 8 only.

# Line Segment 4 (Is4)

- I In the Geometry toolbar, click  $\bigoplus$  More Primitives and choose Line Segment.
- 2 On the object cyll, select Point 4 only.
- 3 In the Settings window for Line Segment, locate the Endpoint section.
- **4** Click to select the **Delta Activate Selection** toggle button for **End vertex**.
- 5 On the object **blk2**, select Point 6 only.
- 6 Click 🟢 Build All Objects.
- 7 Click the Wireframe Rendering button in the Graphics toolbar, and rotate the geometry to get a better view.

Block 3 (blk3)

- I In the **Geometry** toolbar, click 🗍 Block.
- 2 In the Settings window for Block, locate the Size and Shape section.
- 3 In the Width text field, type L.
- 4 In the **Depth** text field, type 2\*R.
- 5 In the **Height** text field, type H.

#### Block 4 (blk4)

- I Right-click Block 3 (blk3) and choose Duplicate.
- 2 In the Settings window for Block, locate the Size and Shape section.
- **3** In the **Depth** text field, type H-6\*R.
- 4 Locate the **Position** section. In the **y** text field, type 6\*R.
- 5 Click 🟢 Build All Objects.

Now, create the final computational domain with a hollow cylinder.

# Difference I (dif1)

- I In the Geometry toolbar, click 📕 Booleans and Partitions and choose Difference.
- 2 Select the objects **blk1** and **blk2** only.
- 3 In the Settings window for Difference, locate the Difference section.
- **4** Click to select the **Delta Activate Selection** toggle button for **Objects to subtract**.
- **5** Select the object **cyll** only.

- 6 In the Geometry toolbar, click 🟢 Build All.
- 7 Click the 🔁 Wireframe Rendering button in the Graphics toolbar. The geometry looks like the following image.
- 8 In the Model Builder window, click Geometry I.



# DEFINITIONS

Variables I

- I In the Home toolbar, click a= Variables and choose Local Variables.
- 2 In the Settings window for Variables, locate the Variables section.
- **3** In the table, enter the following settings:

Name	Expression	Unit	Description
Lct	intop1(-spf.T_stressy/(0.5*spf.rho* (U_mean)^2*(2*R*H)))		Lift coefficient
Ldt	intop1(-spf.T_stressx/(0.5*spf.rho* (U_mean)^2*(2*R*H)))		Drag coefficient
Lcmax	<pre>timemax(0,8,Lct,'nointerp')</pre>		Max lift coefficient
Ldmax	<pre>timemax(0,8,Ldt,'nointerp')</pre>		Max drag coefficient

Name	Expression		Description
Lcmin	<pre>timemin(0,8,Lct,'nointerp')</pre>		Min lift coefficient
Ldmin	<pre>timemin(0,8,Ldt,'nointerp')</pre>		Min drag coefficient
Lcsum	<pre>sqrt(sum((at(k*dt,Lct)-liftref(k* dt))^2,k,0,160))</pre>		Sum of differences, lift coefficient
relLc	<pre>Lcsum/sqrt(sum((liftref(k*dt))^2,k, 0,160))</pre>		Relative error lift coefficient (L2)
Ldsum	<pre>sqrt(sum((at(k*dt,Ldt)-dragref(k* dt))^2,k,0,160))</pre>		Sum of differences, drag coefficient
relLd	Ldsum/sqrt(sum((dragref(k*dt))^2,k, 0,160))		Relative error drag coefficient (L2)

Interpolation 1 (int1)

I In the Home toolbar, click f(x) Functions and choose Local > Interpolation.

Load result files for the lift and drag coefficients to be used for verification.

- 2 In the Settings window for Interpolation, locate the Definition section.
- 3 From the Data source list, choose File.
- 4 Click **Browse**.
- 5 Browse to the model's Application Libraries folder and double-click the file cylinder\_flow\_3d\_periodic\_DragRef.txt.
- 6 Click **[]** Import.
- 7 In the Function name text field, type dragref.

Interpolation 2 (int2)

- I In the Home toolbar, click f(X) Functions and choose Local > Interpolation.
- 2 In the Settings window for Interpolation, locate the Definition section.
- 3 Click 📂 Load from File.
- **4** Browse to the model's Application Libraries folder and double-click the file cylinder\_flow\_3d\_periodic\_LiftRef.txt.

# 5 In the Function name text field, type liftref.

Define operators to verify the results using the imported data.

#### Integration Surface

- I In the Definitions toolbar, click 🗞 Explicit.
- 2 In the Settings window for Explicit, type Integration Surface in the Label text field.
- **3** Locate the **Input Entities** section. From the **Geometric entity level** list, choose **Boundary**.
- **4** Select Boundaries 21–24 only.

# Integration 1 (intop1)

- I In the Definitions toolbar, click A Nonlocal Couplings and choose Integration.
- 2 In the Settings window for Integration, locate the Source Selection section.
- 3 From the Geometric entity level list, choose Boundary.
- 4 From the Selection list, choose Integration Surface.

# Verification Average Operator Domain

- I In the Definitions toolbar, click 🖉 Nonlocal Couplings and choose Average.
- 2 In the Settings window for Average, type Verification Average Operator Domain in the Label text field.
- 3 In the **Operator name** text field, type verificationaveop1.
- 4 Locate the Source Selection section. From the Selection list, choose All domains.

# Verification Maximum Operator Domain

- I In the Definitions toolbar, click / Nonlocal Couplings and choose Maximum.
- 2 In the Settings window for Maximum, type Verification Maximum Operator Domain in the Label text field.
- 3 Locate the Source Selection section. From the Selection list, choose All domains.

# Verification Minimum Operator Domain

- I In the Definitions toolbar, click 🖉 Nonlocal Couplings and choose Minimum.
- 2 In the **Settings** window for **Minimum**, type Verification Minimum Operator Domain in the **Label** text field.
- **3** In the **Operator name** text field, type verificationminop1.
- 4 Locate the Source Selection section. From the Selection list, choose All domains.

# Verification Integration Operator Domain

I In the Definitions toolbar, click 🥖 Nonlocal Couplings and choose Integration.

- 2 In the Settings window for Integration, type Verification Integration Operator Domain in the Label text field.
- 3 In the **Operator name** text field, type verificationintop1.
- 4 Locate the Source Selection section. From the Selection list, choose All domains.

# LAMINAR FLOW (SPF)

- I Click the 🐱 Show More Options button in the Model Builder toolbar.
- 2 In the Show More Options dialog, in the tree, select the checkbox for the node Physics > Stabilization.
- 3 Click OK.
- 4 In the Model Builder window, under Component I (compl) click Laminar Flow (spf).
- **5** In the **Settings** window for **Laminar Flow**, click to expand the **Consistent Stabilization** section.
- 6 Find the Navier-Stokes equations subsection. Clear the Crosswind diffusion checkbox.
- 7 Click to expand the **Discretization** section. From the **Discretization of fluids** list, choose **P2+P2**. **P2+P2** is used because it is more conservative and more accurate than **P2+P1** and **P1+P1**.

Fluid Properties 1

- I In the Model Builder window, under Component I (compl) > Laminar Flow (spf) click Fluid Properties I.
- 2 In the Settings window for Fluid Properties, locate the Fluid Properties section.
- **3** From the  $\rho$  list, choose **User defined**. In the associated text field, type rho.
- 4 From the  $\mu$  list, choose User defined. In the associated text field, type mu.

Inlet 1

- I In the Physics toolbar, click 📄 Boundaries and choose Inlet.
- **2** Select Boundaries 1, 5, and 9 only.
- 3 In the Settings window for Inlet, locate the Velocity section.
- 4 In the  $U_0$  text field, type 36\*U\_mean\*z\*y\*(H-y)\*(H-z)/H^4\*sin(pi\*t/8[s]).

Here, 1/[s] is used to make the input of sin() dimensionless.

#### Outlet I

- I In the Physics toolbar, click 🔚 Boundaries and choose Outlet.
- **2** Select Boundaries 31–33 only.

# MESH I

Use advanced operations such as Map and Sweep to create a hexahedral mesh.

Mapped I

In the Mesh toolbar, click  $\bigwedge$  More Generators and choose Mapped.

## Size

- I In the Model Builder window, click Size.
- 2 In the Settings window for Size, locate the Element Size section.
- 3 From the Calibrate for list, choose Fluid dynamics.
- 4 From the **Predefined** list, choose **Coarse**.

#### Mapped I

- I In the Model Builder window, click Mapped I.
- **2** Select Boundaries 17, 18, 20, and 25 only.

### Distribution I

- I Right-click Mapped I and choose Distribution.
- **2** Select Edges 22, 24, 28, 32, 33, 36, 39, and 46 only.
- 3 In the Settings window for Distribution, click 📗 Build Selected.

## Distribution 2

- I Right-click Mapped I and choose Distribution.
- **2** Select Edges 23 and 27 only.
- 3 In the Settings window for Distribution, locate the Distribution section.
- 4 From the Distribution type list, choose Predefined.
- 5 In the **Element ratio** text field, type 2.
- 6 From the Growth rate list, choose Exponential.

# Distribution 3

- I Right-click Mapped I and choose Distribution.
- **2** Select Edges 40 and 42 only.
- 3 In the Settings window for Distribution, locate the Distribution section.
- 4 From the Distribution type list, choose Predefined.
- 5 In the Element ratio text field, type 2.
- 6 From the Growth rate list, choose Exponential.
- 7 Click 📗 Build All.

# Mapped 2

- I In the Mesh toolbar, click  $\bigwedge$  More Generators and choose Mapped.
- 2 Select Boundaries 8 and 29 only.

## Distribution I

- I Right-click Mapped 2 and choose Distribution.
- 2 Select Edges 9 and 56 only.

### Distribution 2

- I In the Model Builder window, right-click Mapped 2 and choose Distribution.
- **2** Select Edges 10 and 15 only.
- 3 In the Settings window for Distribution, locate the Distribution section.
- 4 From the Distribution type list, choose Predefined.
- 5 In the Number of elements text field, type 8.
- 6 In the **Element ratio** text field, type 3.
- 7 From the Growth rate list, choose Exponential.

#### Distribution 3

- I Right-click Mapped 2 and choose Distribution.
- **2** Select Edges 47 and 50 only.
- 3 In the Settings window for Distribution, locate the Distribution section.
- 4 From the Distribution type list, choose Predefined.
- 5 In the Number of elements text field, type 30.
- 6 In the Element ratio text field, type 6.
- 7 From the Growth rate list, choose Exponential.
- 8 Select the **Reverse direction** checkbox.

#### Mapped 3

- I In the Mesh toolbar, click  $\bigwedge$  More Generators and choose Mapped.
- **2** Select Boundaries 4 and 12 only.

#### Distribution I

- I Right-click Mapped 3 and choose Distribution.
- **2** Select Edges 14 and 59 only.
- 3 In the Settings window for Distribution, locate the Distribution section.
- 4 From the Distribution type list, choose Predefined.

- **5** In the **Element ratio** text field, type **4**.
- 6 From the Growth rate list, choose Exponential.

#### Distribution 2

- I In the Model Builder window, right-click Mapped 3 and choose Distribution.
- 2 Select Edges 4 and 53 only.
- 3 In the Settings window for Distribution, locate the Distribution section.
- 4 From the Distribution type list, choose Predefined.
- 5 In the Element ratio text field, type 4.
- 6 From the Growth rate list, choose Exponential.
- 7 Select the **Reverse direction** checkbox.

# Distribution 3

- I Right-click Mapped 3 and choose Distribution.
- **2** Select Edges 5 and 18 only.
- 3 In the Settings window for Distribution, locate the Distribution section.
- 4 From the Distribution type list, choose Predefined.
- 5 In the Number of elements text field, type 43.
- 6 In the Element ratio text field, type 1.6.
- 7 From the Growth rate list, choose Exponential.

### Swept I

- I In the Mesh toolbar, click A Swept.
- 2 In the Settings window for Swept, click to expand the Source Faces section.
- **3** Select Boundaries 4, 8, 12, 17, 18, 20, 25, and 29 only.
- 4 Click to expand the **Destination Faces** section. Click to clear the **Click to clear** the **C**
- **5** Select Boundaries 3, 7, 11, 16, and 28 only.

#### Distribution I

- I Right-click Swept I and choose Distribution.
- 2 In the Settings window for Distribution, locate the Distribution section.
- 3 From the Distribution type list, choose Predefined.
- 4 In the Number of elements text field, type 10.
- 5 In the Element ratio text field, type 4.

- 6 From the Growth rate list, choose Exponential.
- 7 Select the Symmetric distribution checkbox.
- 8 Click 📗 Build All.

The mesh in Figure 2 is now generated.

# STUDY I

Step 1: Time Dependent

- I In the Model Builder window, under Study I click Step I: Time Dependent.
- 2 In the Settings window for Time Dependent, locate the Study Settings section.
- **3** In the **Output times** text field, type range(0,0.05,8).
- 4 From the Tolerance list, choose User controlled.
- 5 In the Relative tolerance text field, type 0.001.

# Solution 1 (soll)

Choose the generalized alpha method for the time stepping. It has less damping than the BDF.

- I In the Study toolbar, click **here** Show Default Solver.
- 2 In the Model Builder window, expand the Solution I (soll) node.
- 3 In the Model Builder window, under Study I > Solver Configurations > Solution I (soll) click Time-Dependent Solver I.
- **4** In the **Settings** window for **Time-Dependent Solver**, click to expand the **Time Stepping** section.
- 5 From the Method list, choose Generalized alpha.
- 6 Select the Initial step checkbox. In the associated text field, type 0.01.
- 7 From the Maximum step constraint list, choose Constant.
- 8 In the Study toolbar, click **=** Compute.

Evaluate the drag and lift coefficients.

# RESULTS

# Surface 2

- I In the **Results** toolbar, click **More Datasets** and choose **Surface**.
- **2** Select Boundaries 21–24 only.

#### Integral I

- I In the **Results** toolbar, click **More Datasets** and choose **Evaluation** > **Integral**.
- 2 In the Settings window for Integral, locate the Data section.
- 3 From the Dataset list, choose Surface 2.

#### Point Evaluation 1

- I In the **Results** toolbar, click  $\frac{8.85}{e-12}$  **Point Evaluation**.
- 2 In the Settings window for Point Evaluation, locate the Data section.
- 3 From the Dataset list, choose Integral I.
- **4** Locate the **Expressions** section. In the table, enter the following settings:

Expression	Unit	Description
-spf.T_stressy/(0.5*spf.rho*(U_mean)^2* (2*R*H))	1	Lift coefficient
-spf.T_stressx/(0.5*spf.rho*(U_mean)^2* (2*R*H))	1	Drag coefficient

5 Click **=** Evaluate.

# TABLE I

- I Go to the Table I window.
- 2 Click the Table Graph button in the window toolbar.

# TABLE I

- I Go to the Table I window.
- 2 Click the Table Graph button in the window toolbar.

Plot the lift coefficient versus time as shown in Figure 4.

- 3 In the Settings window for Table Graph, locate the Data section.
- 4 From the Plot columns list, choose Manual.
- 5 In the Columns list, select Lift coefficient (1), Integral 1.

#### RESULTS

# Lift coefficient

- I In the Model Builder window, under Results click ID Plot Group 3.
- 2 In the Settings window for ID Plot Group, type Lift coefficient in the Label text field.
- 3 Locate the Plot Settings section.

4 Select the y-axis label checkbox. In the associated text field, type c<sub>L</sub>.

#### Drag coefficient

Plot the drag coefficient versus time as shown in Figure 5.

- I Right-click Lift coefficient and choose Duplicate.
- 2 In the Settings window for ID Plot Group, type Drag coefficient in the Label text field.
- 3 Locate the Plot Settings section. In the y-axis label text field, type c<sub>D</sub>.

#### Table Graph 1

- I In the Model Builder window, expand the Drag coefficient node, then click Table Graph I.
- 2 In the Settings window for Table Graph, locate the Data section.
- 3 In the Columns list, select Drag coefficient (1), Integral I.
- **4** In the **Drag coefficient** toolbar, click **I** Plot.

# Point Evaluation 1

Evaluate the maximum and minimum of the coefficients.

#### Point Evaluation 2

- I In the Model Builder window, under Results > Derived Values right-click Point Evaluation I and choose Duplicate.
- 2 In the Settings window for Point Evaluation, locate the Data Series Operation section.
- 3 From the Transformation list, choose Maximum.
- **4** Click **•** next to **= Evaluate**, then choose **New Table**.

#### Point Evaluation 3

- I Right-click Point Evaluation 2 and choose Duplicate.
- 2 In the Settings window for Point Evaluation, locate the Expressions section.
- **3** Click to select row number 2 in the table.
- 4 Right-click and choose **Delete**.
- 5 Locate the Data Series Operation section. From the Transformation list, choose Minimum.
- 6 Click next to = Evaluate, then choose Table 2 Point Evaluation 2.

# Surface 3

- I In the **Results** toolbar, click **More Datasets** and choose **Surface**.
- 2 Select Boundaries 2, 13, and 21–24 only.

Now, visualize the velocity field as shown in Figure 3.

# Velocity (spf)

- I In the Model Builder window, under Results click Velocity (spf).
- 2 In the Settings window for 3D Plot Group, locate the Color Legend section.
- 3 Clear the Show legends checkbox.
- 4 Locate the Plot Settings section. Clear the Plot dataset edges checkbox.
- **5** Locate the **Data** section. From the **Time (s)** list, choose **7.95**. Since the inlet velocity vanishes at the final time step, the solution at t=7.95s is chosen for a better visualization of the streamlines.

#### Slice

Create a slice in the middle of the computational domain, parallel to the xy – plane to see the flow pattern more clearly.

- I In the Model Builder window, expand the Velocity (spf) node, then click Slice.
- 2 In the Settings window for Slice, locate the Plane Data section.
- 3 From the Plane list, choose xy-planes.
- 4 In the Planes text field, type 1.
- **5** Locate the **Coloring and Style** section. From the **Color table** list, choose **JupiterAuroraBorealis**.

#### Deformation 1

Shift the slice back to the wall to get a better view.

- I Right-click Slice and choose Deformation.
- 2 In the Settings window for Deformation, locate the Expression section.
- **3** In the **z-component** text field, type -0.205.
- 4 Locate the Scale section.
- **5** Select the **Scale factor** checkbox. In the associated text field, type **1**.

#### Streamline 1

Create and add arrows to the streamlines.

- I In the Model Builder window, right-click Velocity (spf) and choose Streamline.
- 2 In the Settings window for Streamline, locate the Streamline Positioning section.
- **3** In the **Number** text field, type 10.
- **4** Select Boundaries 1, 5, and 9 only.
- **5** Locate the **Coloring and Style** section. Find the **Line style** subsection. From the **Type** list, choose **Tube**.

- 6 Select the Radius scale factor checkbox. In the associated text field, type 0.003.
- 7 Find the Point style subsection. From the Type list, choose Arrow.
- 8 From the Color list, choose Custom.
- **9** On Windows, click the colored bar underneath, or if you are running the crossplatform desktop — the **Color** button.
- **IO** Click **Define custom colors**.
- II Set the RGB values to 71, 145, and 199, respectively.
- 12 Click Add to custom colors.
- 13 Click Show color palette only or OK on the cross-platform desktop.

Surface 1

- I Right-click Velocity (spf) and choose Surface.
- 2 In the Settings window for Surface, locate the Data section.
- 3 From the Dataset list, choose Surface 3.
- 4 Locate the Expression section. In the Expression text field, type 1.
- 5 Locate the Coloring and Style section. From the Coloring list, choose Uniform.
- 6 From the Color list, choose Gray.

Evaluation Group 1

- I In the **Results** toolbar, click **Levaluation Group**.
- 2 In the Settings window for Evaluation Group, locate the Data section.
- **3** From the **Time selection** list, choose **Last**.

Global Evaluation 1

- I Right-click Evaluation Group I and choose Global Evaluation.
- 2 In the Settings window for Global Evaluation, locate the Expressions section.
- **3** In the table, enter the following settings:

Expression	Unit	Description
Lcmax	1	Max lift coefficient
Lcmin	1	Min lift coefficient
Ldmax	1	Max drag coefficient
relLc	1	Relative error lift coefficient (L2)
relLd	1	Relative error drag coefficient (L2)

**4** In the **Evaluation Group I** toolbar, click **= Evaluate**.